

4.2 p. 269 #'s 63 + 71

63.) $f(x) = \frac{2x}{3x-1}$

① change x 's to y 's + vice versa

$$x = \frac{2y}{3y-1}$$

Domain of $f = \{x | x \neq \frac{1}{3}\}$

② mult each side by $(3y-1)$ + distribute

Range of $f = \{y | y \neq \frac{2}{3}\}$

$$(3y-1)x = \frac{2y}{3y-1} (3y-1)$$

*Hint: The range of $f =$ the domain of f^{-1} .

$$3xy - x = 2y$$

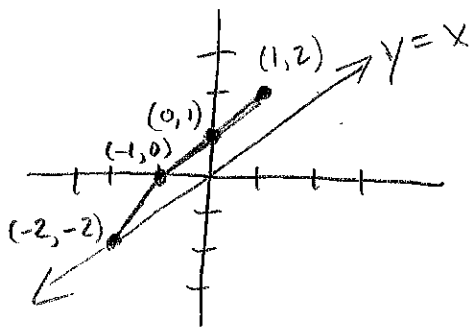
③ Put any term w/ a y on the left side + everything else on the right, then factor out a y on the left side and solve for y .

$$3xy - 2y = x$$

$$\frac{y(3x-2)}{3x-2} = \frac{x}{3x-2}$$

$$f^{-1}(x) = \frac{x}{3x-2}$$

71.) use graph from #31 on p. 268



a.) $f(-1) = 0$ (when $x = -1$, what is y ?)

b.) $f(1) = 2$ (when $x = 1$, what is y ?)

c.) $f^{-1}(1) = 0$ (when $y = 1$, what is x ?)

d.) $f^{-1}(2) = 1$ (when $y = 2$, what is x ?)